IN THE CLAIMS

Please amend claims 1, 2, 4, 17 and 20, and add claims 21-25 as follows:

- 1. (Currently Amended) A linear method for performing head
- 2 motion estimation from facial feature data, the method comprising
- 3 the steps of:
- obtaining a first facial image and detecting a head in said
- 5 first image;
- detecting position of not more than four points P of said
- first facial image where $P = \{\mathbf{p}_1, \mathbf{p}_2, \mathbf{p}_3, \mathbf{p}_4\}$, and $\mathbf{p}_k = (\mathbf{x}_k, \mathbf{y}_k)$;
- 8 obtaining a second facial image and detecting a head in said
- 9 second image;
- detecting position of not more than four points P' of said
- 11 first facial image where $P' = \{\mathbf{p}_1', \mathbf{p}_2', \mathbf{p}_3', \mathbf{p}_4'\}$ and $\mathbf{p}_k' = (x_k', y_k') +$; and
- determining the motion of the head represented by a rotation
- matrix R and translation vector T using said points P and P'.
 - 2. (Currently Amended) The linear method of claim 1, wherein
- 2 said four points P of said first facial image and said four points

- 3 P' of said second facial image include locations of outer corners
- 4 of each eye and mouth of each respective first and second facial
- 5 images.
- 3. (Original) The linear method of claim 1, wherein said head
- 2 motion estimation is governed according to:

$$\mathbf{P}_i' = R\mathbf{P}_i + \mathbf{T}$$
, where $R = \begin{bmatrix} \mathbf{r}_1^T \\ \mathbf{r}_2^T \\ \mathbf{r}_3^T \end{bmatrix} = \begin{bmatrix} r_{ij} \end{bmatrix}_{3\times 3}$ and $\mathbf{T} = \begin{bmatrix} T_1 & T_2 & T_3 \end{bmatrix}^T$ represent camera

- 4 rotation and translation respectively, said head pose estimation
- 5 being a specific instance of head motion estimation.
- 4. (Currently Amended) The linear method of claim 3 A linear
- method for performing head motion estimation from facial feature
- data, the method comprising the steps of:
- obtaining a first facial image and detecting a head in said
- 5 first image;
- detecting position of four points P of said first facial image
- where $P = \{\mathbf{p}_1, \mathbf{p}_2, \mathbf{p}_3, \mathbf{p}_4\}$, and $\mathbf{p}_k = (\mathbf{x}_k, \mathbf{y}_k)$;
- obtaining a second facial image and detecting a head in said
- 9 second image;

- detecting position of four points P' of said first facial
- image where $P' = \{\mathbf{p}'_1, \mathbf{p}'_2, \mathbf{p}'_3, \mathbf{p}'_4\}$ and $\mathbf{p}'_k = (x'_k, y'_k)$; and,
- determining the motion of the head represented by a rotation
- matrix R and translation vector T using said points P and P',
- wherein said head motion estimation is governed according to:

$$\underline{\mathbf{P}_{i}' = R\mathbf{P}_{i} + \mathbf{T}}_{, \text{ where }} R = \begin{bmatrix} \mathbf{r}_{1}^{T} \\ \mathbf{r}_{2}^{T} \\ \mathbf{r}_{3}^{T} \end{bmatrix} = \begin{bmatrix} \mathbf{r}_{ij} \end{bmatrix}_{3\times 3} \underline{\quad \text{and }} \mathbf{T} = \begin{bmatrix} T_{1} & T_{2} & T_{3} \end{bmatrix}^{T} \underline{\quad \text{represent camera}}$$

- 16 rotation and translation respectively, said head pose estimation
- 17 being a specific instance of head motion estimation, and
- wherein said head motion estimation is governed according to
- 19 said rotation matrix R, said method further comprising the steps
- 20 of:
- determining rotation matrix R that maps points P_k to F_k for
- characterizing a head pose, said points F_1, F_2, F_3, F_4 representing three-
- 23 dimensional (3-D) coordinates of the respective four points of a
- 24 reference, frontal view of said facial image, and P_k is the three-
- 25 dimensional (3-D) coordinates of an arbitrary point where
- 26 $\mathbf{P}_i = [X_i \ Y_i \ Z_i]^T$, said mapping governed according to the relation:

$$R(\mathbf{P}_2 - \mathbf{P}_1) \propto \begin{bmatrix} 1 & 0 & 0 \end{bmatrix}^T$$

$$R(\mathbf{P}_6 - \mathbf{P}_5) \propto \begin{bmatrix} 0 & 1 & 0 \end{bmatrix}^T$$

- wherein P_5 and P_6 are midpoints of respective line segments connecting points P_1P_2 and P_3P_4 and, line segment connecting points
- P_1P_2 is orthogonal to a line segment connecting points P_5P_6 , and
- 33 [∞]indicates a proportionality factor.
- 5. (Original) The linear method of claim 4, wherein components r1, r2 and r3 are computed as:

$$\mathbf{r}_{2}^{T}(\mathbf{P}_{2} - \mathbf{P}_{1}) = 0$$

$$\mathbf{r}_{3}^{T}(\mathbf{P}_{2} - \mathbf{P}_{1}) = 0$$

$$\mathbf{r}_{1}^{T}(\mathbf{P}_{6} - \mathbf{P}_{5}) = 0$$

$$\mathbf{r}_{3}^{T}(\mathbf{P}_{6} - \mathbf{P}_{5}) = 0$$

- 6. (Original) The linear method of claim 5, wherein
- 2 components r1, r2 and r3 are computed as:

$$r_3 = (P_6 - P_5) \times (P_2 - P_1)$$
,

$$\mathbf{r}_{2} = \mathbf{r}_{3} \times (\mathbf{P}_{2} - \mathbf{P}_{1})$$

$$\mathbf{r}_{1} = \mathbf{r}_{2} \times \mathbf{r}_{3}$$

7. (Original) The linear method of claim 4, wherein

$$\begin{bmatrix} \mathbf{P}_i^T & \mathbf{0}^T & \mathbf{0}^T & 1 & 0 & 0 \\ \mathbf{0}^T & \mathbf{P}_i^T & \mathbf{0}^T & 0 & 1 & 0 \\ \mathbf{0}^T & \mathbf{0}^T & \mathbf{P}_i^T & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \mathbf{r}_1 \\ \mathbf{r}_2 \\ \mathbf{r}_3 \\ \mathbf{T} \end{bmatrix} = \mathbf{P}_i'$$

- each point pair yielding 3 equations, whereby at least four
- 4 point pairs are necessary to linearly solve for said rotation and
- 5 translation.

- 8. (Original) The linear method of claim 7, further comprising
- 2 the step of: decomposing said rotation matrix R using Singular
- 3 Value Decomposition (SVD) to obtain a form $R = USV^{T}$.
- 9. (Original) The linear method of claim 7, further comprising
- the step of computing a new rotation matrix according to $R = UV^T$.
- 1 10.(Original) A linear method for performing head motion
- 2 estimation from facial feature data, the method comprising the
- 3 steps of:
- obtaining image position of four points P_k of a facial image;

determining a rotation matrix R that maps points \mathbf{P}_k to \mathbf{F}_k for

- characterizing a head pose, said points $\mathbf{F}_1, \mathbf{F}_2, \mathbf{F}_3, \mathbf{F}_4$ representing
- 7 three-dimensional (3-D) coordinates of the respective four points
- 8 of a reference, frontal view of said facial image, and P_k is the
- 9 three-dimensional (3-D) coordinates of an arbitrary point where
- $\mathbf{P}_i = \begin{bmatrix} X_i & Y_i & Z_i \end{bmatrix}^T$, said mapping governed according to the relation:

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$$R(\mathbf{P}_2 - \mathbf{P}_1) \propto \begin{bmatrix} 1 & 0 & 0 \end{bmatrix}^T$$

$$R(\mathbf{P}_6 - \mathbf{P}_5) \propto \begin{bmatrix} 0 & 1 & 0 \end{bmatrix}^T$$

- wherein P_5 and P_6 are midpoints of respective line segments
- connecting points P_1P_2 and P_3P_4 and, line segment connecting points
- 16 P_1P_2 is orthogonal to a line segment connecting points P_5P_6 , and
- 17 α indicates a proportionality factor.
- 1 11.(Original) The linear method of claim 10, wherein
- 2 components r1, r2 and r3 are computed as:

$$\mathbf{r}_2^T(\mathbf{P}_2 - \mathbf{P}_1) = 0$$

$$\mathbf{r}_3^T(\mathbf{P}_2 - \mathbf{P}_1) = 0$$

$$\mathbf{r}_1^T(\mathbf{P}_6 - \mathbf{P}_5) = 0$$

$$\mathbf{r}_3^T(\mathbf{P}_6 - \mathbf{P}_5) = 0$$

- 12. (Original) The linear method of claim 11, wherein 1
- components r1, r2 and r3 are computed as: 2

$$\mathbf{r}_3 = (\mathbf{P}_6 - \mathbf{P}_5) \times (\mathbf{P}_2 - \mathbf{P}_1),$$

$$\mathbf{r}_2 = \mathbf{r}_3 \times (\mathbf{P}_2 - \mathbf{P}_1)$$

$$\mathbf{r}_1 = \mathbf{r}_2 \times \mathbf{r}_3$$

- The linear method of claim 12, wherein a motion 13. (Original) 1
- of head points is represented according to $P'_i = RP_i + T$ 2

$$R = \begin{bmatrix} \mathbf{r}_1^T \\ \mathbf{r}_2^T \\ \mathbf{r}_3^T \end{bmatrix} = \begin{bmatrix} r_{ij} \end{bmatrix}_{3\times 3}$$
where represents image rotation, $\mathbf{T} = \begin{bmatrix} T_1 & T_2 & T_3 \end{bmatrix}^T$

- represents translation, and \mathbf{P}_i' denotes a 3-D image position of four
- points P_k of another facial image 5
- 14.(Original) The linear method of claim 13, wherein 1

$$\begin{bmatrix}
\mathbf{P}_{i}^{T} & \mathbf{0}^{T} & \mathbf{0}^{T} & 1 & 0 & 0 \\
\mathbf{0}^{T} & \mathbf{P}_{i}^{T} & \mathbf{0}^{T} & 0 & 1 & 0 \\
\mathbf{0}^{T} & \mathbf{0}^{T} & \mathbf{P}_{i}^{T} & 0 & 0 & 1
\end{bmatrix}
\begin{bmatrix}
\mathbf{r}_{1} \\
\mathbf{r}_{2} \\
\mathbf{r}_{3} \\
\mathbf{T}
\end{bmatrix} = \mathbf{P}_{i}^{\prime},$$

- each point pair yielding 3 equations, whereby at least four
- 4 point pairs are necessary to linearly solve for said rotation and
- 5 translation.
- 1 15. (Original) The linear method of claim 14, further
- 2 comprising the step of: decomposing said rotation matrix R using
- 3 Singular Value Decomposition (SVD) to obtain a form $R = USV^{T}$.
- 1 16.(Original) The linear method of claim 15, further
- 2 comprising the step of computing a new rotation matrix according to
- $R = UV^T$.
- 1 17. (Currently Amended) A program storage device readable by
- 2 machine, tangible embodying a program of instructions executable by
- 3 the machine to perform method steps for performing head motion
- 4 estimation from facial feature data, the method comprising the
- steps of:
- obtaining a first facial image and detecting a head in said
- 7 first image;

- detecting position of not more than four points P of said
- 9 first facial image where $P = \{p_1, p_2, p_3, p_4\}$, and $p_k = (x_k, y_k)$;
- obtaining a second facial image and detecting a head in said
- 11 second image;
- detecting position of not more than four points P' of said
- first facial image where $P' = \{\mathbf{p}_1', \mathbf{p}_2', \mathbf{p}_3', \mathbf{p}_4'\}$ and $\mathbf{p}_k' = (x_k', y_k') + ;$ and,
- determining the motion of the head represented by a rotation
- matrix R and translation vector T using said points P and P'.
- 1 18. (Original) The program storage device readable by machine
- 2 as claimed in claim 17, wherein said four points P of said first
- 3 facial image and four points P' of said second facial image include
- 4 locations of outer corners of each eye and mouth of each respective
- 5 first and second facial image.
- 1 19. (Original) The program storage device readable by machine
- 2 as claimed in claim 17, wherein said head motion estimation is
- 3 governed according to:

Amendment in Reply to Office Action of September 27, 2004

$$R = \begin{bmatrix} \mathbf{r}_1^T \\ \mathbf{r}_2^T \\ \mathbf{r}_3^T \end{bmatrix} = \begin{bmatrix} r_{ij} \end{bmatrix}_{3\times 3}$$

$$\mathbf{T} = \begin{bmatrix} T_1 & T_2 & T_3 \end{bmatrix}^T \text{ represent}$$

- 5 camera rotation and translation respectively, said head pose
- 6 estimation being a specific instance of head motion estimation.
- 20. (Currently Amended) The A program storage device readable
- 2 by machine as claimed in claim 19, tangible embodying a program of
- 3 instructions executable by the machine to perform method steps for
- 4 performing head motion estimation from facial feature data, the
- 5 method comprising the steps of:
- obtaining a first facial image and detecting a head in said
- 7 first image;
- 8 detecting position of four points P of said first facial image
- where $P = \{P_1, P_2, P_3, P_4\}$, and $P_k = (x_k, y_k)$;
- obtaining a second facial image and detecting a head in said
- 11 second image;
- detecting position of four points P' of said first facial
- image where $P' = \{\mathbf{p}'_1, \mathbf{p}'_2, \mathbf{p}'_3, \mathbf{p}'_4\}$ and $\mathbf{p}'_k = (x'_k, y'_k)$; and

- determining the motion of the head represented by a rotation
- matrix R and translation vector T using said points P and P',
- wherein said head motion estimation is governed according to:

$$R = \begin{bmatrix} \mathbf{r}_1^T \\ \mathbf{r}_2^T \\ \mathbf{r}_3^T \end{bmatrix} = \begin{bmatrix} r_{ij} \end{bmatrix}_{3\times 3}$$

$$\mathbf{P}_i' = R\mathbf{P}_i + \mathbf{T}_i \quad \text{where} \quad \mathbf{T} = \begin{bmatrix} T_1 & T_2 & T_3 \end{bmatrix}^T \text{ represent}$$

- 18 camera rotation and translation respectively, said head pose
- 19 estimation being a specific instance of head motion estimation, and
- wherein said head pose estimation is governed according to
- 21 said rotation matrix R, said method further comprising the steps
- 22 of:
- determining rotation matrix R that maps points P_k to F_k for
- characterizing a head pose, said points F_1, F_2, F_3, F_4 representing three-
- 25 dimensional (3-D) coordinates of the respective four points of a
- reference, frontal view of said facial image-, and P_k is the three-
- 27 dimensional (3-D) coordinates of an arbitrary point where
- 28 $\mathbf{P}_i = \begin{bmatrix} X_i & Y_i & Z_i \end{bmatrix}^T$, said mapping governed according to the relation:

$$R(\mathbf{P}_2 - \mathbf{P}_1) \propto \begin{bmatrix} 1 & 0 & 0 \end{bmatrix}^T$$

$$R(\mathbf{P}_6 - \mathbf{P}_5) \propto \begin{bmatrix} 0 & 1 & 0 \end{bmatrix}^T$$

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wherein P_5 and P_6 are midpoints of respective line segments connecting points P_1P_2 and P_3P_4 and, line segment connecting points P_1P_2 is orthogonal to a line segment connecting points P_5P_6 , and

1 21.(New) The program storage device readable by machine as

 ∞ indicates a proportionality factor.

- claimed in claim 20, wherein components r1, r2 and r3 are computed
- 3 as:

$$\mathbf{r}_{2}^{T}(\mathbf{P}_{2} - \mathbf{P}_{1}) = 0$$

$$\mathbf{r}_{3}^{T}(\mathbf{P}_{2} - \mathbf{P}_{1}) = 0$$

$$\mathbf{r}_{1}^{T}(\mathbf{P}_{6} - \mathbf{P}_{5}) = 0$$

$$\mathbf{r}_{3}^{T}(\mathbf{P}_{6} - \mathbf{P}_{5}) = 0$$

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- 1 22.(New) The program storage device readable by machine as
- 2 claimed in claim 20, wherein components r1, r2 and r3 are computed
- 3 as:

$$\mathbf{r}_3 = (\mathbf{P}_6 - \mathbf{P}_5) \times (\mathbf{P}_2 - \mathbf{P}_1),$$

$$\mathbf{r}_2 = \mathbf{r}_3 \times (\mathbf{P}_2 - \mathbf{P}_1)$$

$$\mathbf{r}_1 = \mathbf{r}_2 \times \mathbf{r}_3$$

23.(New) The program storage device readable by machine as claimed in claim 20, wherein

$$\begin{bmatrix} \mathbf{P}_i^T & \mathbf{0}^T & \mathbf{0}^T & 1 & 0 & 0 \\ \mathbf{0}^T & \mathbf{P}_i^T & \mathbf{0}^T & 0 & 1 & 0 \\ \mathbf{0}^T & \mathbf{0}^T & \mathbf{P}_i^T & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \mathbf{r}_1 \\ \mathbf{r}_2 \\ \mathbf{r}_3 \\ \mathbf{T} \end{bmatrix} = \mathbf{P}_i'$$

- each point pair yielding 3 equations, whereby at least four
 point pairs are necessary to linearly solve for said rotation and
 translation.
 - 24.(New) The program storage device readable by machine as claimed in claim 23, further comprising the steps of decomposing said rotation matrix R using Singular Value Decomposition (SVD) to obtain a form $R = USV^T$.
 - 25.(New) The program storage device readable by machine as claimed in claim 23, further comprising the steps of computing a new rotation matrix according to $R = UV^T$.